

CS462 Image Processing

Chapter 6

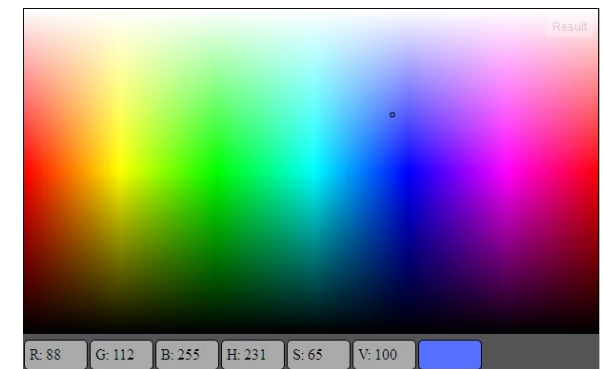
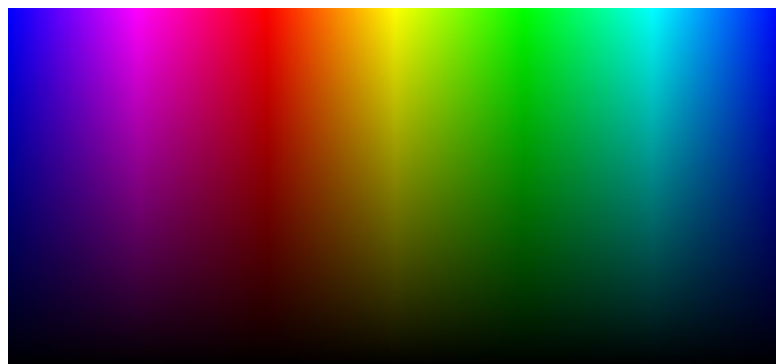
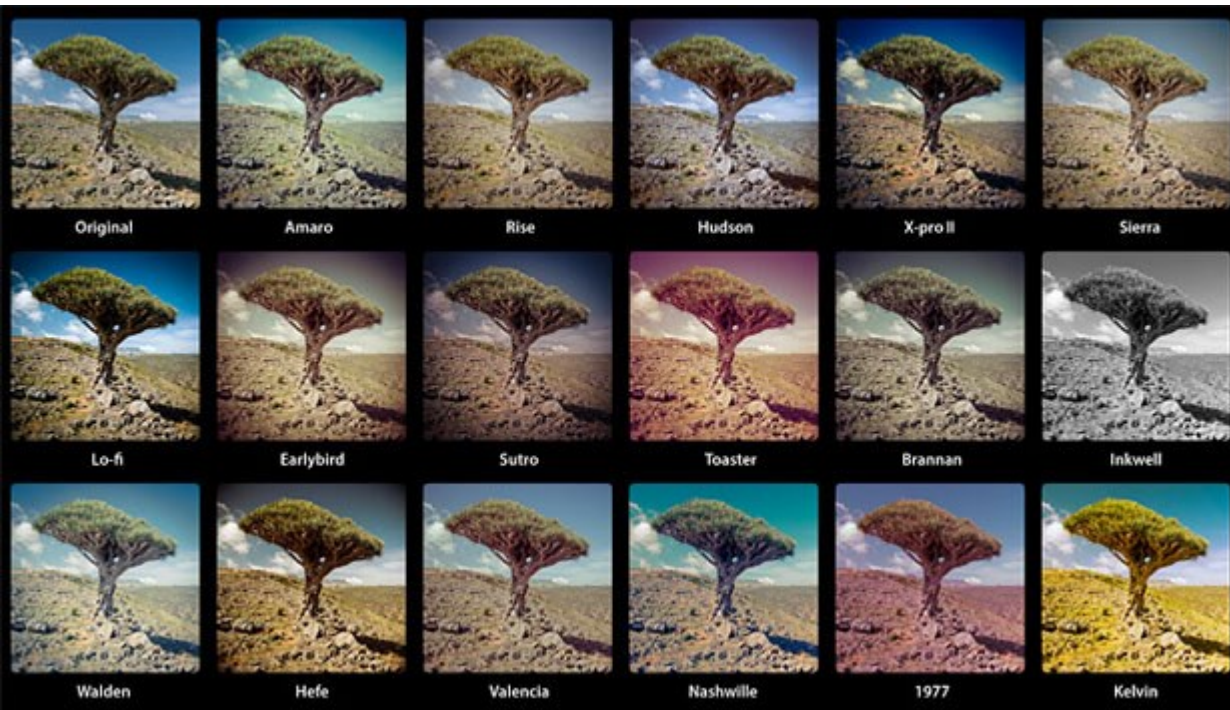
Colours

By Dr. Paween Khoenkaw

Computer Science MJU



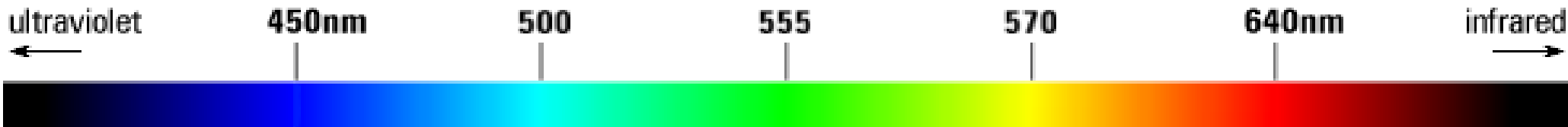
Color Processing



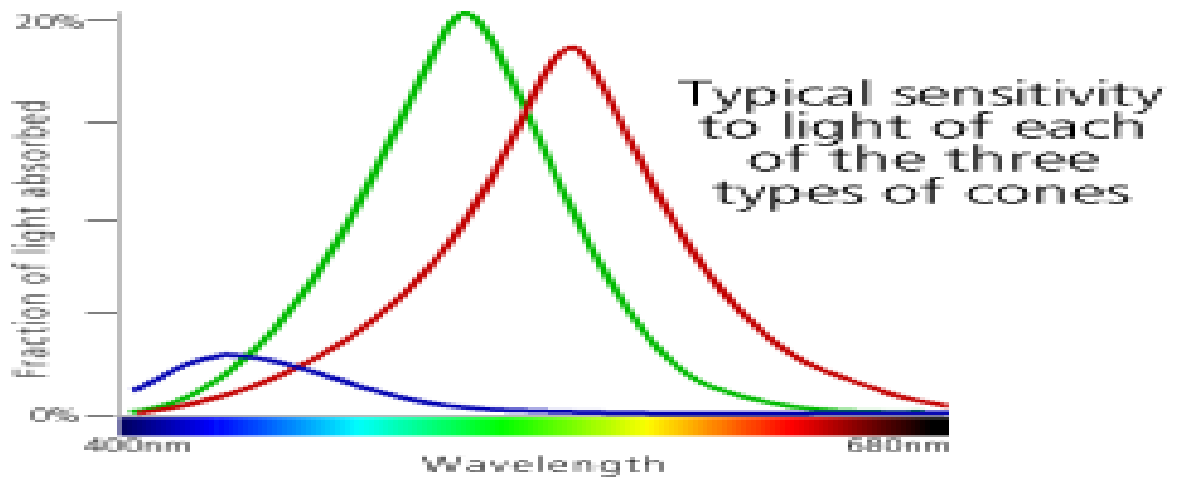
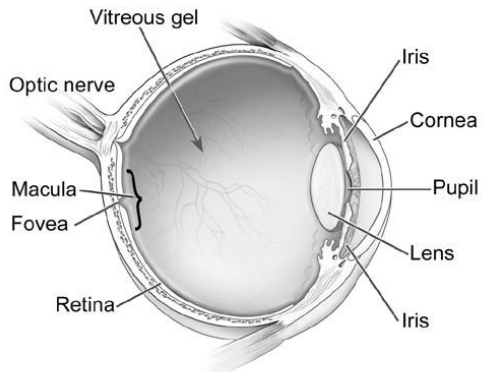
What is color ?

The colors of the visible light spectrum

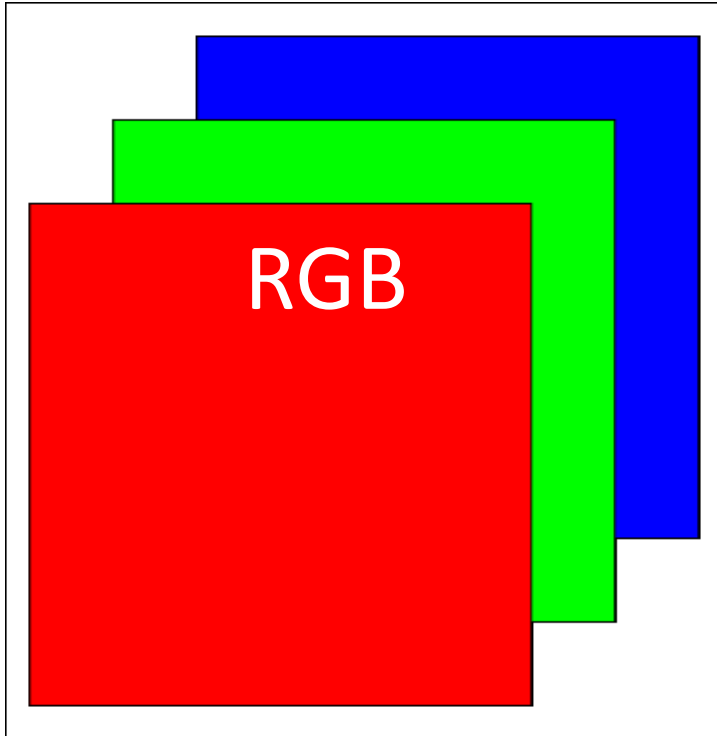
color	wavelength interval	frequency interval
red	~ 700–635 nm	~ 430–480 THz
orange	~ 635–590 nm	~ 480–510 THz
yellow	~ 590–560 nm	~ 510–540 THz
green	~ 560–520 nm	~ 540–580 THz
cyan	~ 520–490 nm	~ 580–610 THz
blue	~ 490–450 nm	~ 610–670 THz
violet	~ 450–400 nm	~ 670–750 THz



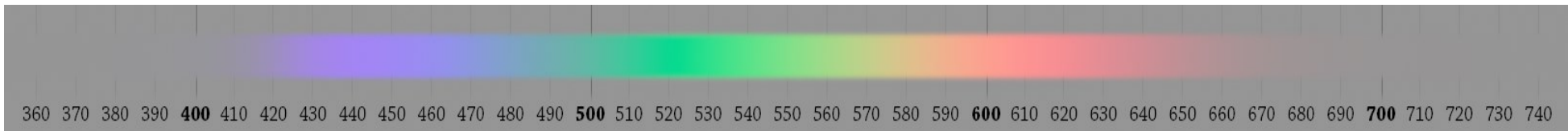
Where is purple ?



Colors

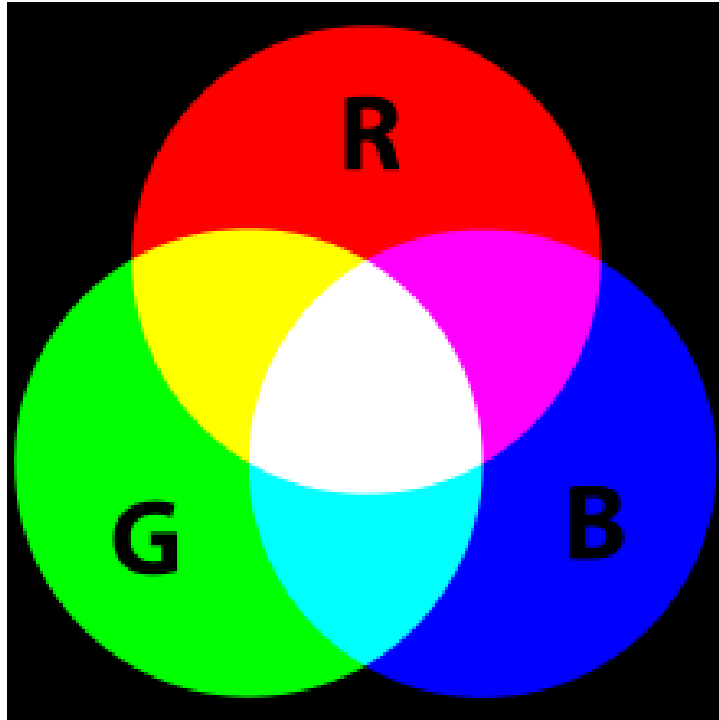


The colors of the visible light spectrum		
color	wavelength interval	frequency interval
red	~ 700–635 nm	~ 430–480 THz
orange	~ 635–590 nm	~ 480–510 THz
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blue	~ 490–450 nm	~ 610–670 THz
violet	~ 450–400 nm	~ 670–750 THz



Colors

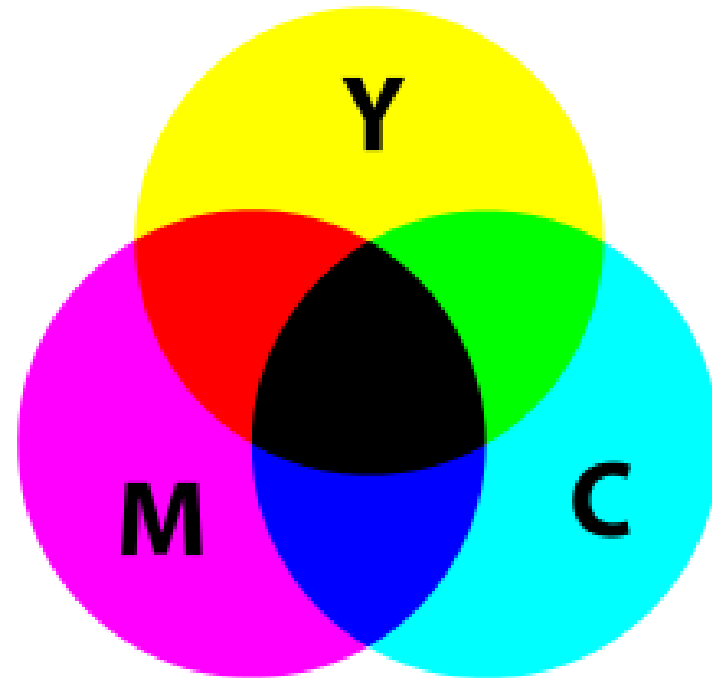
Additive



$$\text{Color} = R + G + B$$



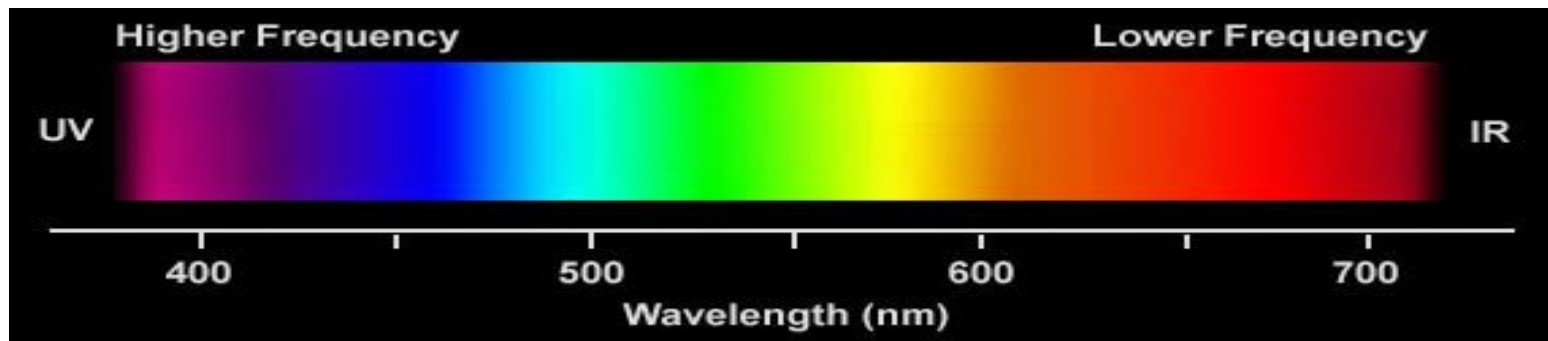
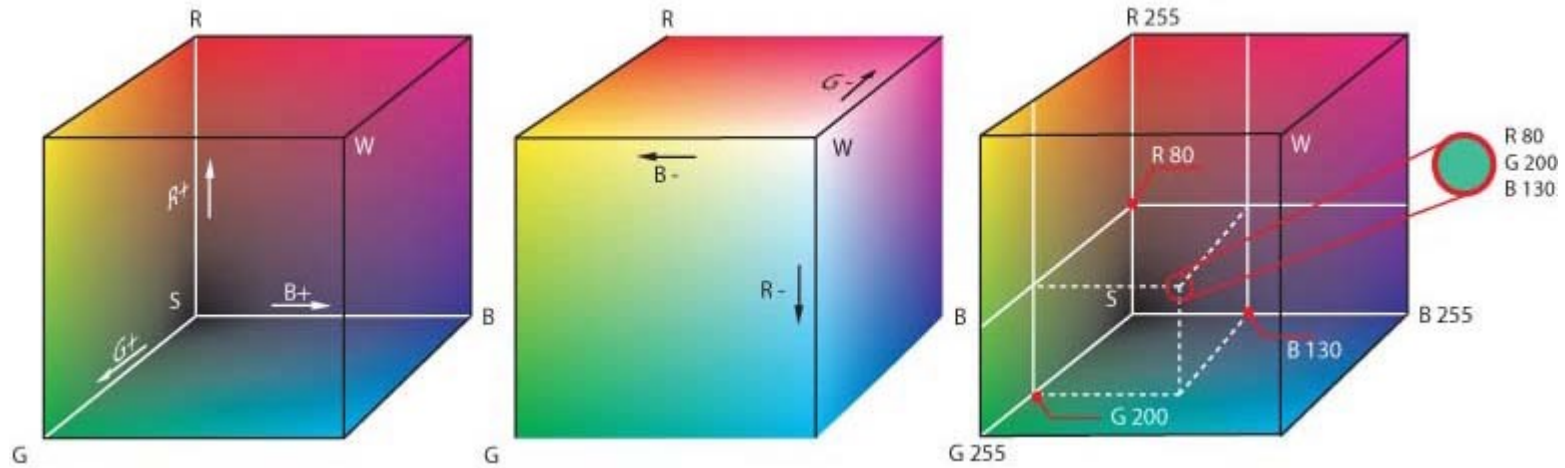
Subtractive



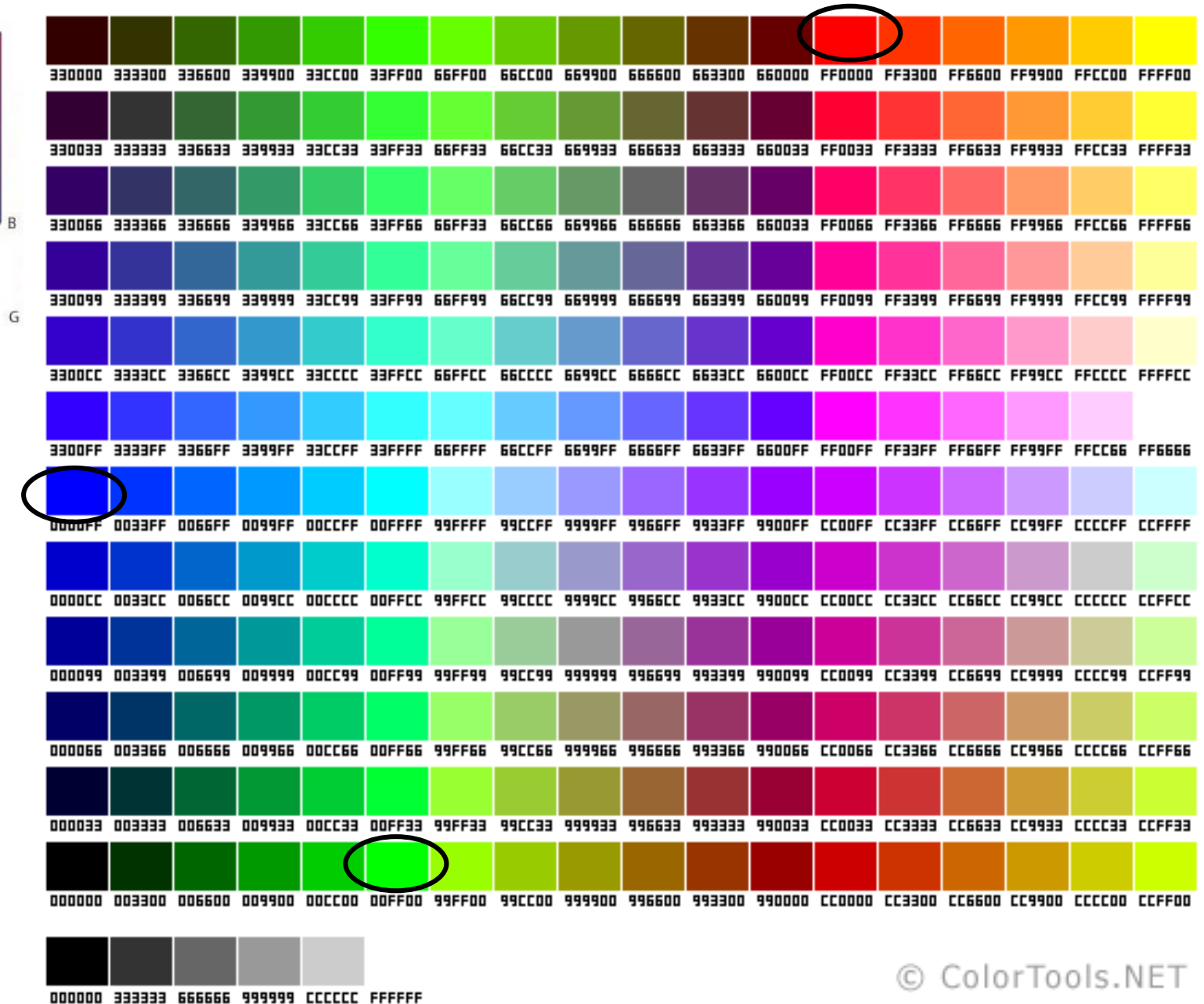
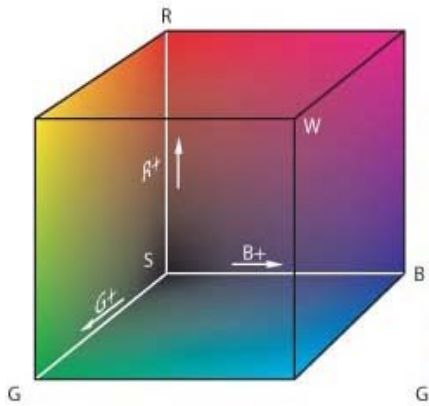
$$\text{Color} = 1 - C - M - Y$$



RGB Color space



RGB Colors Mixing



© ColorTools.NET

RR GG BB

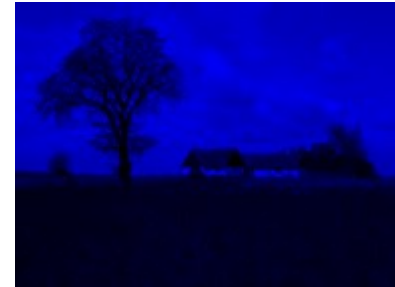
RGB Colors Mixing



-0



-60



-70



RGB Colors Mixing



$$.393R+.769G+.189B$$



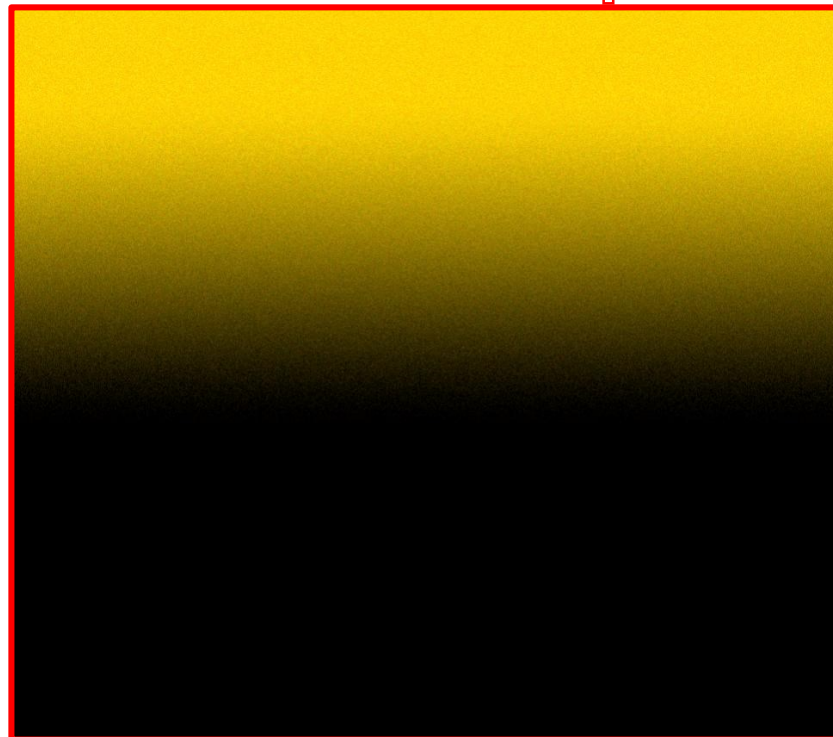
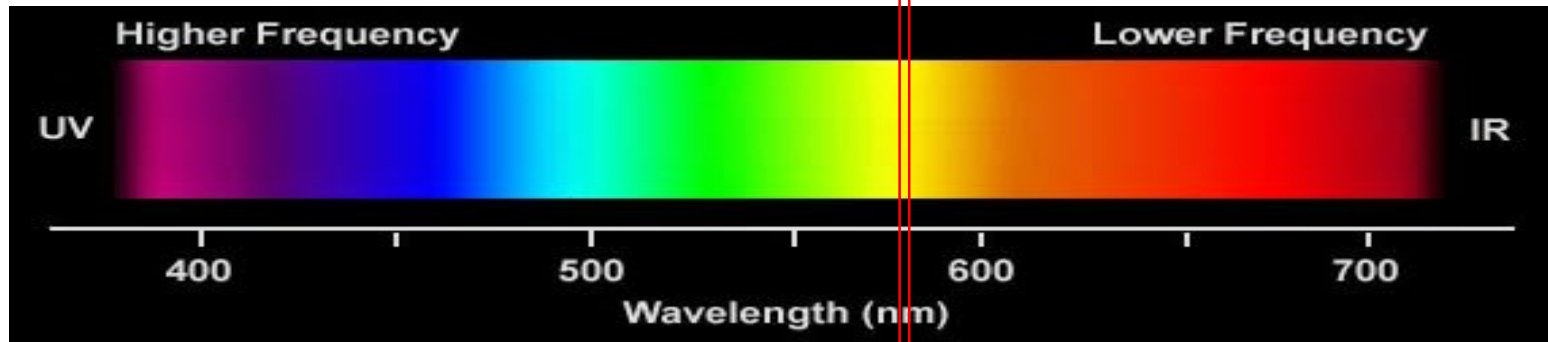
$$.349R+.686G+.168B$$



$$.272R+.534G+.131B$$



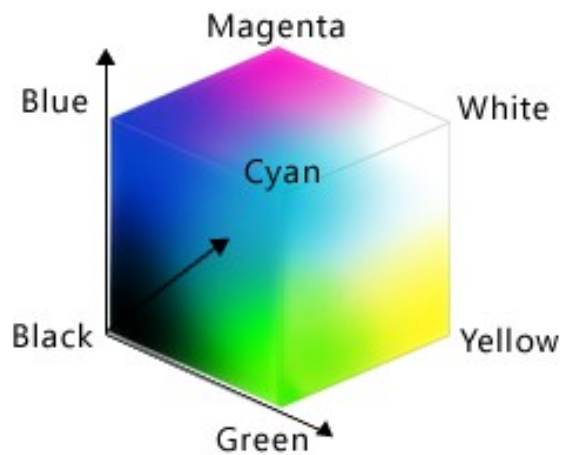
RGB Color in difference brightness



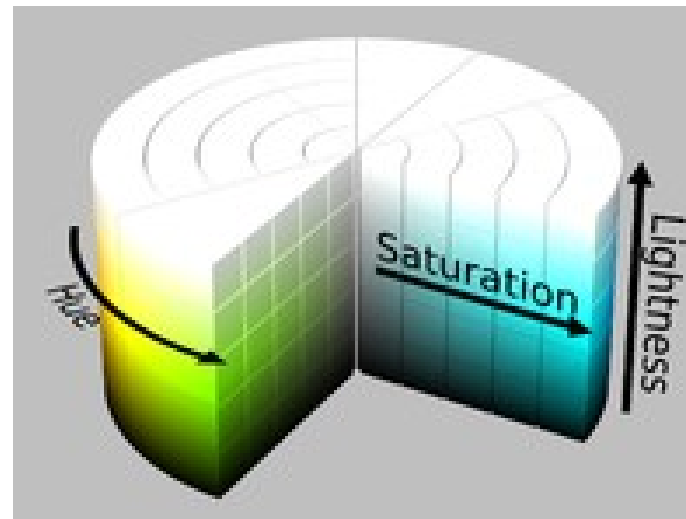
HSL and HSV Color space

HSL stands for Hue, Saturation, and Lightness

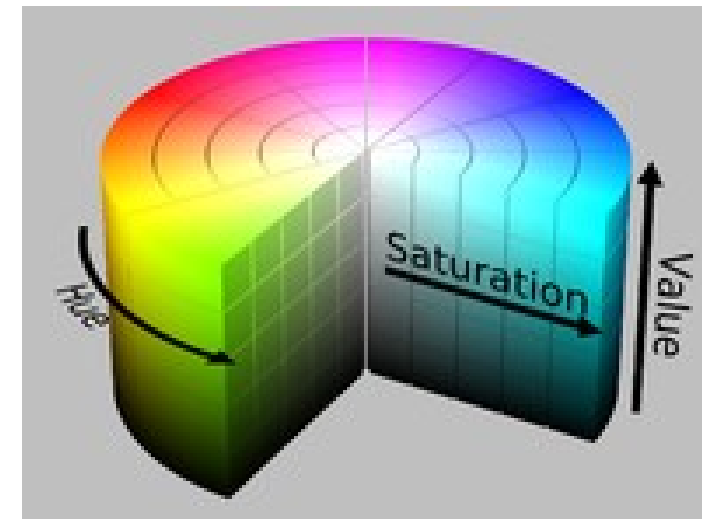
HSV stands for Hue, Saturation, and Value



RGB



HSL



HSV

HSV Color space



RED



GREEN



BLUE



HUE



SATURATION



Color VALUE

HSV Color space



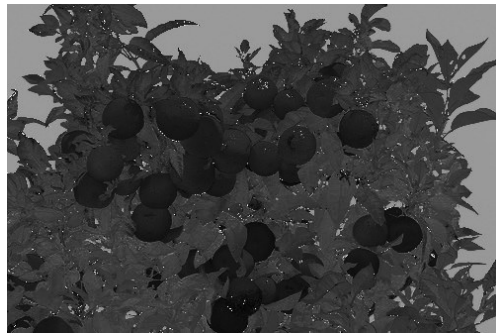
RED



GREEN



BLUE



HUE

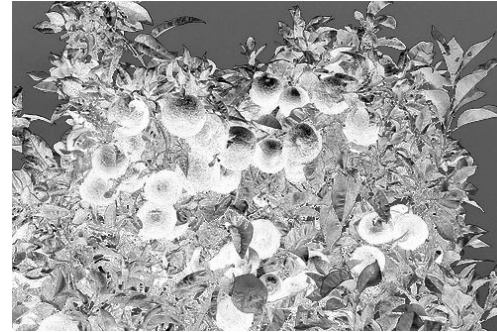
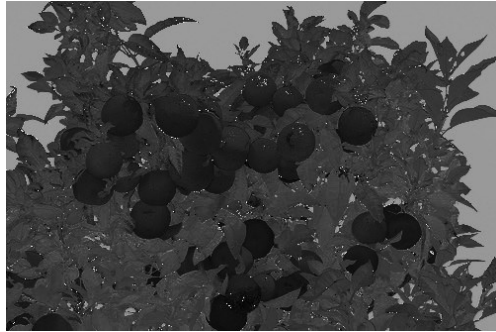


SATURATION



Color VALUE

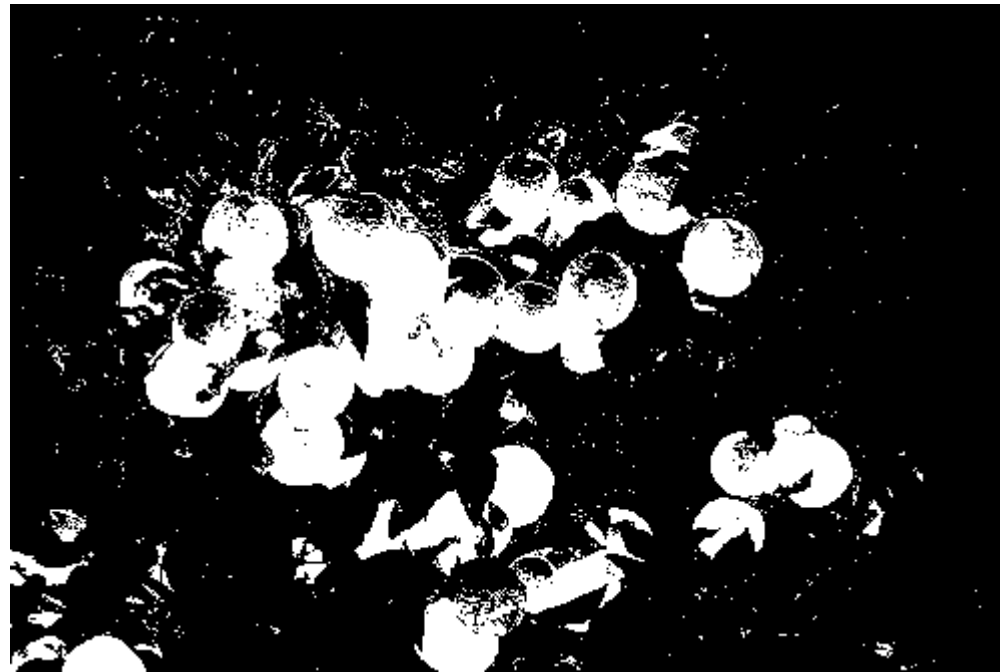
HSV Color space



HUE

SATURATION

Color VALUE



$$Im_{binary} = (Hue < 0.15) \wedge (Saturation > 0.5)$$

Convert RGB space to HSV space

$$C_{max} = \max\{r, g, b\} \quad C_{min} = \min\{r, g, b\}$$

$$\Delta = C_{max} - C_{min}$$

$$H = \begin{cases} 0^\circ, & \Delta = 0 \\ 60^\circ \times \left(\frac{g - b}{\Delta} \bmod 6 \right) \times \frac{1}{360}, & C_{max} = r \\ 60^\circ \times \left(\frac{b - r}{\Delta} + 2 \right) \times \frac{1}{360}, & C_{max} = g \\ 60^\circ \times \left(\frac{r - g}{\Delta} + 4 \right) \times \frac{1}{360}, & C_{max} = b \end{cases}$$

$$S = \begin{cases} 0, & C_{max} = 0 \\ \frac{\Delta}{C_{max}}, & C_{max} \neq 0 \end{cases} \quad V = \frac{C_{max}}{255}$$

Convert RGB space to HSV space

$$C_{max} = \max\{r, g, b\}$$

$$C_{min} = \min\{r, g, b\}$$

$$\Delta = C_{max} - C_{min}$$

$$H = \begin{cases} 0^\circ & , \Delta = 0 \\ 60^\circ \times \left(\frac{g - b}{\Delta} \bmod 6 \right) \times \frac{1}{360} & , C_{max} = r \\ 60^\circ \times \left(\frac{b - r}{\Delta} + 2 \right) \times \frac{1}{360} & , C_{max} = g \\ 60^\circ \times \left(\frac{r - g}{\Delta} + 4 \right) \times \frac{1}{360} & , C_{max} = b \end{cases}$$

$$S = \begin{cases} 0 & , C_{max} = 0 \\ \frac{\Delta}{C_{max}} & , C_{max} \neq 0 \end{cases}$$

$$V = \frac{C_{max}}{255}$$



R=64, G=50, B=110

H=? , S=? , V=?

Convert RGB space to HSV space

R=64,G=50,B=110

$$C_{max} = \max\{r, g, b\}$$

$$C_{min} = \min\{r, g, b\}$$

$$\Delta = C_{max} - C_{min}$$

$$H = \begin{cases} 0^\circ, & \Delta = 0 \\ 60^\circ \times \left(\frac{g-b}{\Delta} \bmod 6\right) \times \frac{1}{360}, & C_{max} = r \\ 60^\circ \times \left(\frac{b-r}{\Delta} + 2\right) \times \frac{1}{360}, & C_{max} = g \\ 60^\circ \times \left(\frac{r-g}{\Delta} + 4\right) \times \frac{1}{360}, & C_{max} = b \end{cases}$$

$$S = \begin{cases} 0, & C_{max} = 0 \\ \frac{\Delta}{C_{max}}, & C_{max} \neq 0 \end{cases}$$

$$V = \frac{C_{max}}{255}$$

$$C_{max} = \max\{64, 50, 110\}$$

$$C_{max} = 110$$

$$C_{min} = \min\{64, 50, 110\}$$

$$C_{min} = 50$$

$$\Delta = 110 - 50 = 60$$

$$H = \begin{cases} 0^\circ, & \Delta = 0 \\ 60^\circ \times \left(\frac{g-b}{\Delta} \bmod 6\right) \times \frac{1}{360}, & C_{max} = r \\ 60^\circ \times \left(\frac{b-r}{\Delta} + 2\right) \times \frac{1}{360}, & C_{max} = g \\ 60^\circ \times \left(\frac{r-g}{\Delta} + 4\right) \times \frac{1}{360}, & C_{max} = b \end{cases}$$

$$H = 60^\circ \times \left(\frac{64 - 50}{60} + 4\right) \times \frac{1}{360}$$

$$H = 0.7055$$

$$S = \frac{60}{110} = 0.5454$$

$$V = \frac{110}{255} = 0.4314$$

Convert HSV space to RGB space

$$C = V \times S$$

$$X = C \times \left(1 - \left|1 - \left(\frac{H \times 60}{360}\right) \bmod 2 - 1\right|\right)$$

$$m = V - C$$

$$\{R', G', B'\} = \begin{cases} (C, X, 0) & , 0 \leq H < 0.1667 \\ (X, C, 0) & , 0.1667 \leq H < 0.3333 \\ (0, C, X) & , 0.3333 \leq H < 0.5 \\ (0, X, C) & , 0.5 \leq H < 0.6667 \\ (X, 0, C) & , 0.6667 \leq H < 0.8333 \\ (C, 0, X) & , 0.8333 \leq H < 1 \end{cases}$$

$$\{R, G, B\} = \{(R' + m), (G' + m), (B' + m)\}$$

Convert HSV space to RGB space

$$C = V \times S$$

$$X = C \times \left(1 - \left|1 - \left(\frac{H \times 60}{360}\right) \bmod 2 - 1\right|\right)$$

$$m = V - C$$

$$\{R', G', B'\} = \begin{cases} (C, X, 0) & , 0 \leq H < 0.1667 \\ (X, C, 0) & , 0.1667 \leq H < 0.3333 \\ (0, C, X) & , 0.3333 \leq H < 0.5 \\ (0, X, C) & , 0.5 \leq H < 0.6667 \\ (X, 0, C) & , 0.6667 \leq H < 0.8333 \\ (C, 0, X) & , 0.8333 \leq H < 1 \end{cases}$$

$$\{R, G, B\} = \{(R' + m), (G' + m), (B' + m)\}$$

H=0.7055, S=0.5454, V=0.4314



R=?, **G=?**, **B=?**

Convert HSV space to RGB space

$$C = V \times S$$

$$X = C \times \left(1 - \left|1 - \left(\frac{H \times 60}{360}\right) \bmod 2 - 1\right|\right)$$

$$m = V - C$$

$$\{R', G', B'\} = \begin{cases} (C, X, 0) & , 0 \leq H < 0.1667 \\ (X, C, 0) & , 0.1667 \leq H < 0.3333 \\ (0, C, X) & , 0.3333 \leq H < 0.5 \\ (0, X, C) & , 0.5 \leq H < 0.6667 \\ (X, 0, C) & , 0.6667 \leq H < 0.8333 \\ (C, 0, X) & , 0.8333 \leq H < 1 \end{cases}$$

$$\{R, G, B\} = \{(R' + m), (G' + m), (B' + m)\}$$

$$H=0.7055, S=0.5454, V=0.4314$$

$$C = 0.4314 \times 0.5454$$

$$C = 0.2352$$

$$X = 0.2352 \times \left(1 - \left|1 - \left(\frac{0.7055 \times 60}{360}\right) \bmod 2 - 1\right|\right)$$

$$X = 0.0548$$

$$m = 0.4314 - 0.2352$$

$$m = 0.1962$$

$$\{R', G', B'\} = \begin{cases} (C, X, 0) & , 0 \leq H < 0.1667 \\ (X, C, 0) & , 0.1667 \leq H < 0.3333 \\ (0, C, X) & , 0.3333 \leq H < 0.5 \\ (0, X, C) & , 0.5 \leq H < 0.6667 \\ (X, 0, C) & , 0.6667 \leq H < 0.8333 \\ (C, 0, X) & , 0.8333 \leq H < 1 \end{cases}$$

$$\{R', G', B'\} = \{0.0548, 0, 0.2352\}$$

$$R = 0.0548 + 0.1962 = 0.251$$

$$G = 0 + 0.1962 = 0.1962$$

$$B = 0.2352 + 0.1962 = 0.4314$$

Convert HSV space to RGB space

$$C = V \times S$$

$$X = C \times \left(1 - \left|1 - \left(\frac{H \times 60}{360}\right) \bmod 2 - 1\right|\right)$$

$$m = V - C$$

$$\{R', G', B'\} = \begin{cases} (C, X, 0) & , 0 \leq H < 0.1667 \\ (X, C, 0) & , 0.1667 \leq H < 0.3333 \\ (0, C, X) & , 0.3333 \leq H < 0.5 \\ (0, X, C) & , 0.5 \leq H < 0.6667 \\ (X, 0, C) & , 0.6667 \leq H < 0.8333 \\ (C, 0, X) & , 0.8333 \leq H < 1 \end{cases}$$

$$\{R, G, B\} = \{(R' + m), (G' + m), (B' + m)\}$$

$$H=0.7055, S=0.5454, V=0.4314$$

$$C = 0.4314 \times 0.5454$$

$$C = 0.2352$$

$$X = 0.2352 \times \left(1 - \left|1 - \left(\frac{0.7055 \times 60}{360}\right) \bmod 2 - 1\right|\right)$$

$$X = 0.0548$$

$$m = 0.4314 - 0.2352$$

$$m = 0.1962$$

$$\{R', G', B'\} = \begin{cases} (C, X, 0) & , 0 \leq H < 0.1667 \\ (X, C, 0) & , 0.1667 \leq H < 0.3333 \\ (0, C, X) & , 0.3333 \leq H < 0.5 \\ (0, X, C) & , 0.5 \leq H < 0.6667 \\ (X, 0, C) & , 0.6667 \leq H < 0.8333 \\ (C, 0, X) & , 0.8333 \leq H < 1 \end{cases}$$

$$\{R', G', B'\} = \{0.0548, 0, 0.2352\}$$

$$R = 0.251 \times 255 = 64.005$$

$$G = 0.1962 \times 255 = 50.031$$

$$B = 0.4314 \times 255 = 110.007$$

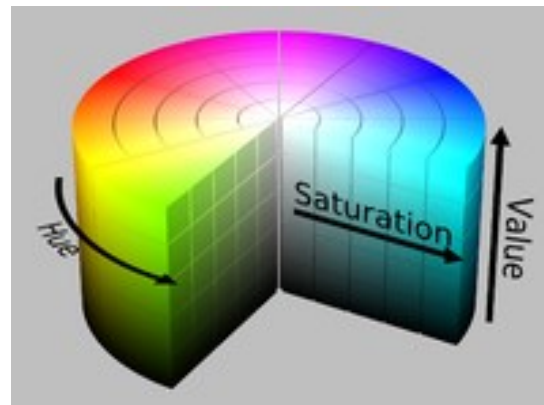
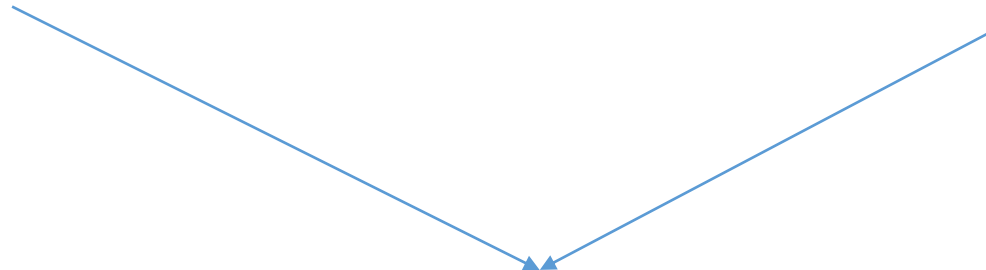
HSV Color Mixing



H

S

V



HSV Color Mixing

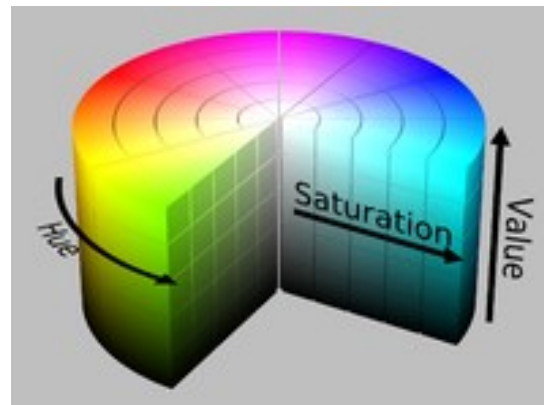


H

S

V

X 0.3



HSV Color Mixing

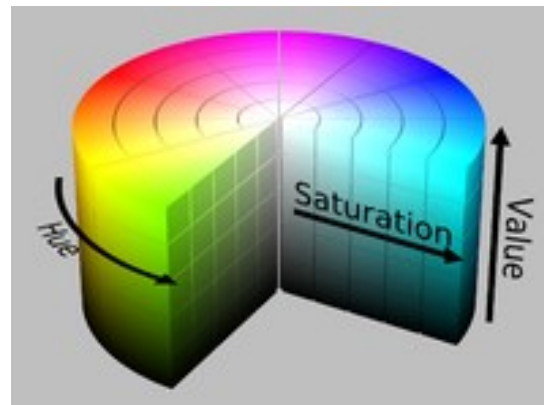


H

S

V

X 2



HSV Color Mixing

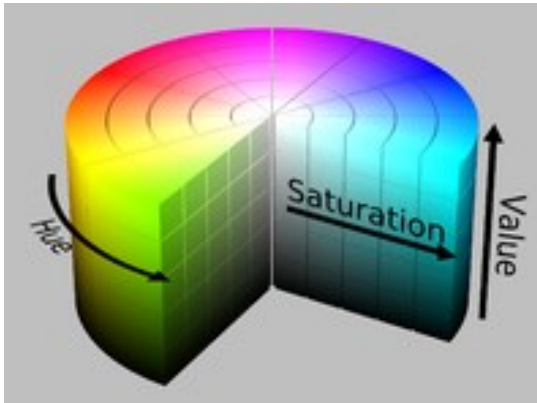


H

S

V

X 0.3



HSV Color Mixing

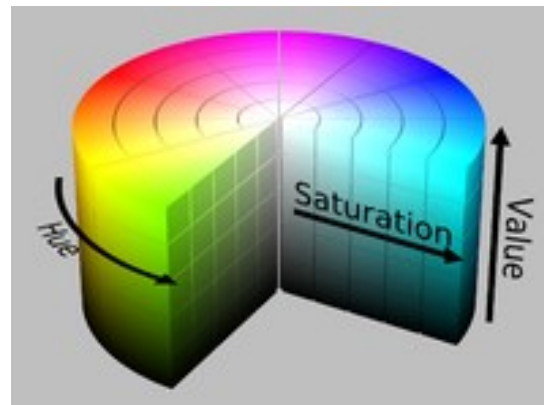


H

S

V

X 2



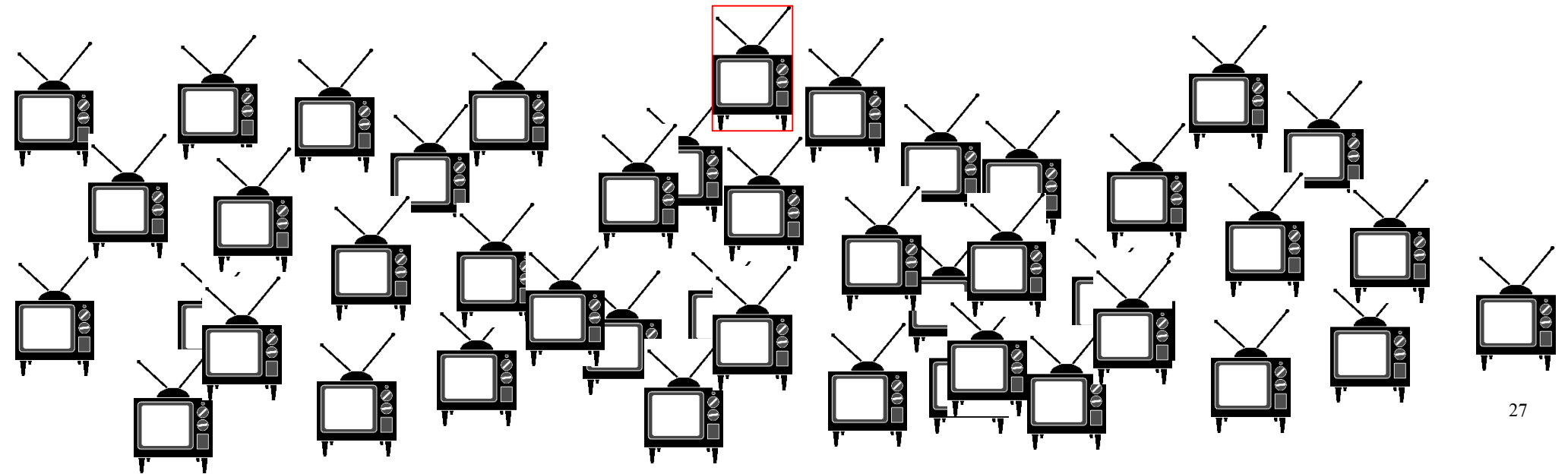
YUV Color Space



Black and White Television



Color Television



YUV Color Space



Gray



R



G



B



Original Image

Bandwidth x4



V



S



H



Original Image

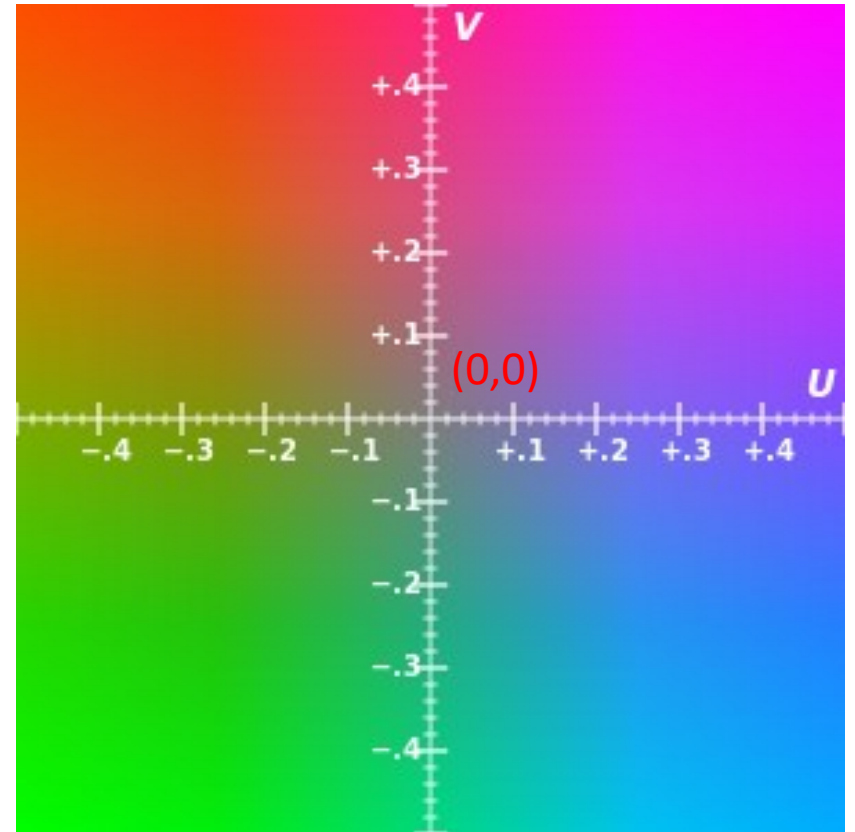
Bandwidth x3

Shades are wrong

YUV Color Space



Gray (Y)



U-V color plane



U



V



Y + U + V

YUV Color Space

SDTV with BT.601

$$Y = 0.299R + 0.587G + 0.114B$$

$$U = (-0.14713R - 0.28886G + 0.436B)$$

$$V = (0.615R - 0.51499G - 0.10001B)$$

$$\begin{bmatrix} Y \\ U \\ V \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ -0.14713 & -0.28886 & 0.436 \\ 0.615 & -0.51499 & -0.10001 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

$$\begin{bmatrix} R \\ G \\ B \end{bmatrix} = \begin{bmatrix} 1 & 0 & 1.13983 \\ 1 & -0.39465 & -0.58060 \\ 1 & 2.03211 & 0 \end{bmatrix} \begin{bmatrix} Y \\ U \\ V \end{bmatrix}$$

YUV Color Mixing

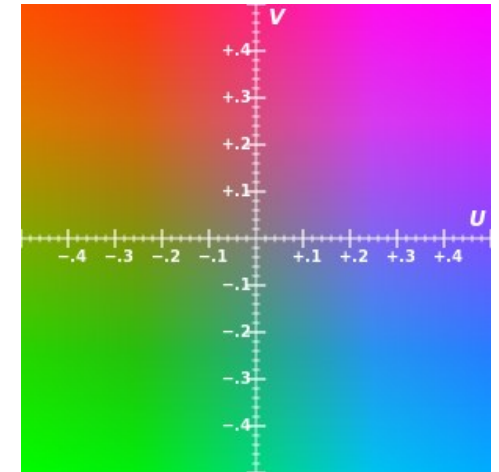


Y

U

V

$\times 0.5$



YUV Color Mixing

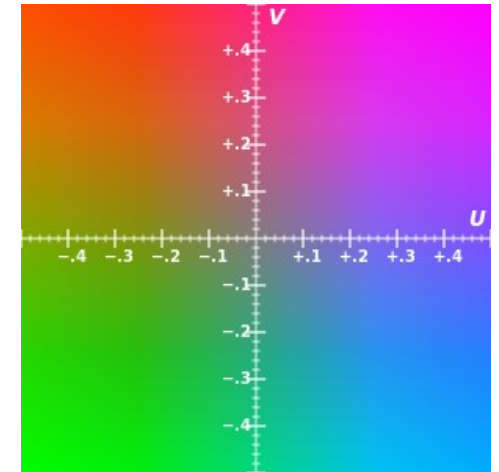


Y

U

V

X2



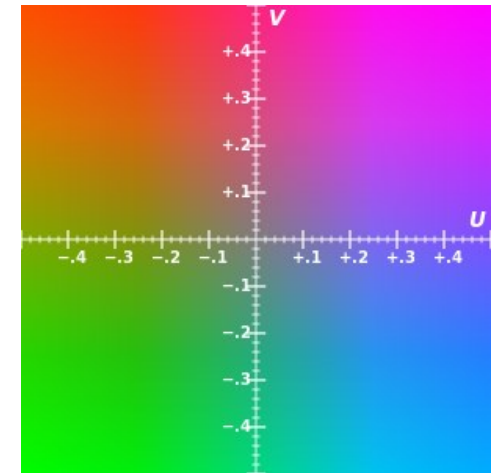
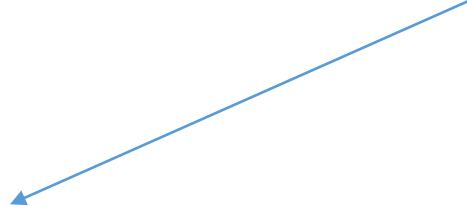
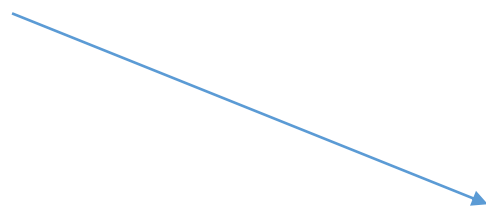
YUV Color Mixing



Y

U

V



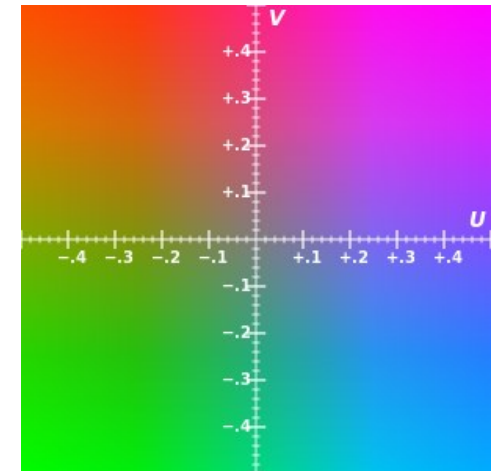
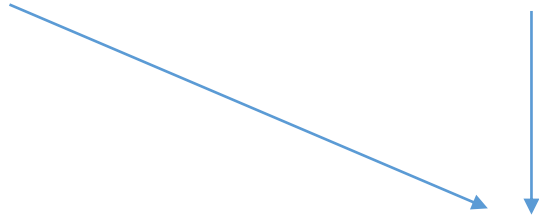
YUV Color Mixing



Y

U

V



YUV Color Mixing

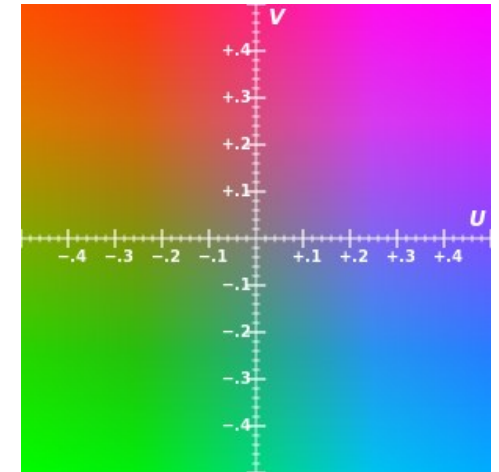


Y

U

V

-128



YUV Color Mixing

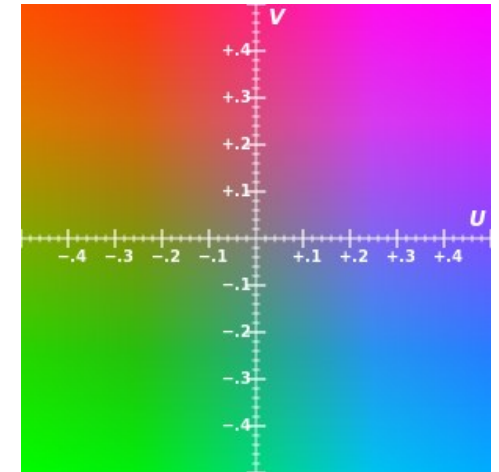


Y

U

V

-128



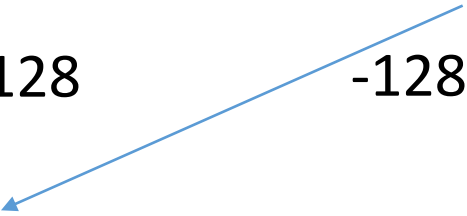
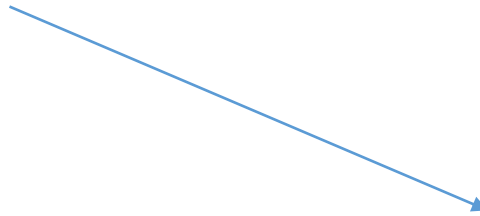
YUV Color Mixing



Y

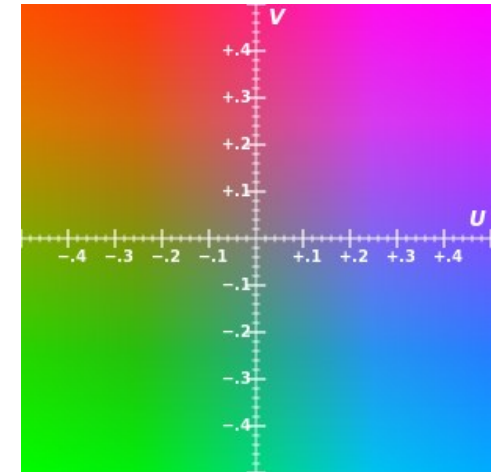
U

V



-128

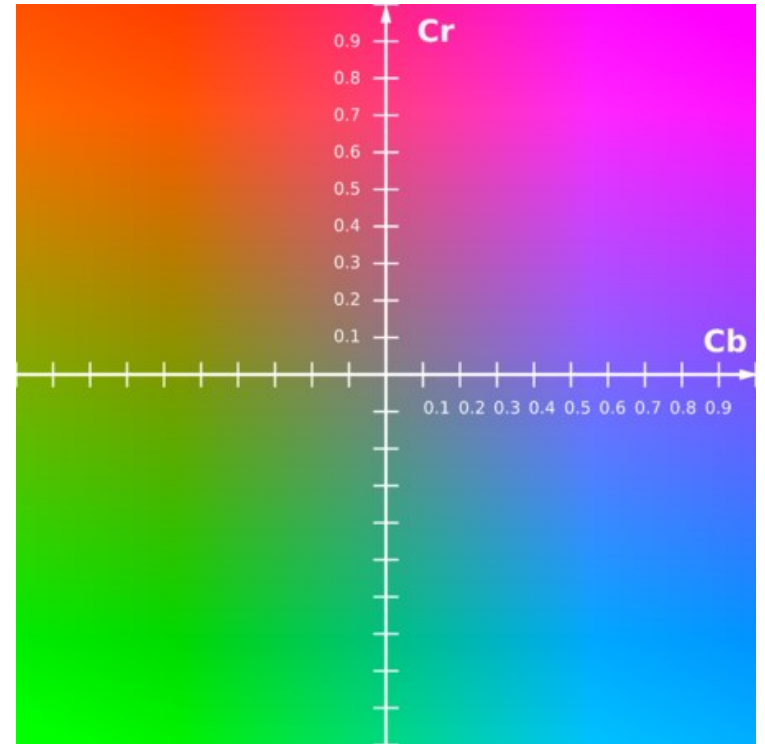
-128



YCbCr Color Space



Y



Cb



Cr

YCbCr Color Space

JPEG conversion

$$Y = 0.299R + 0.587G + 0.114B$$

$$Cb = 128 - 0.168736R - 0.331264G + 0.5B$$

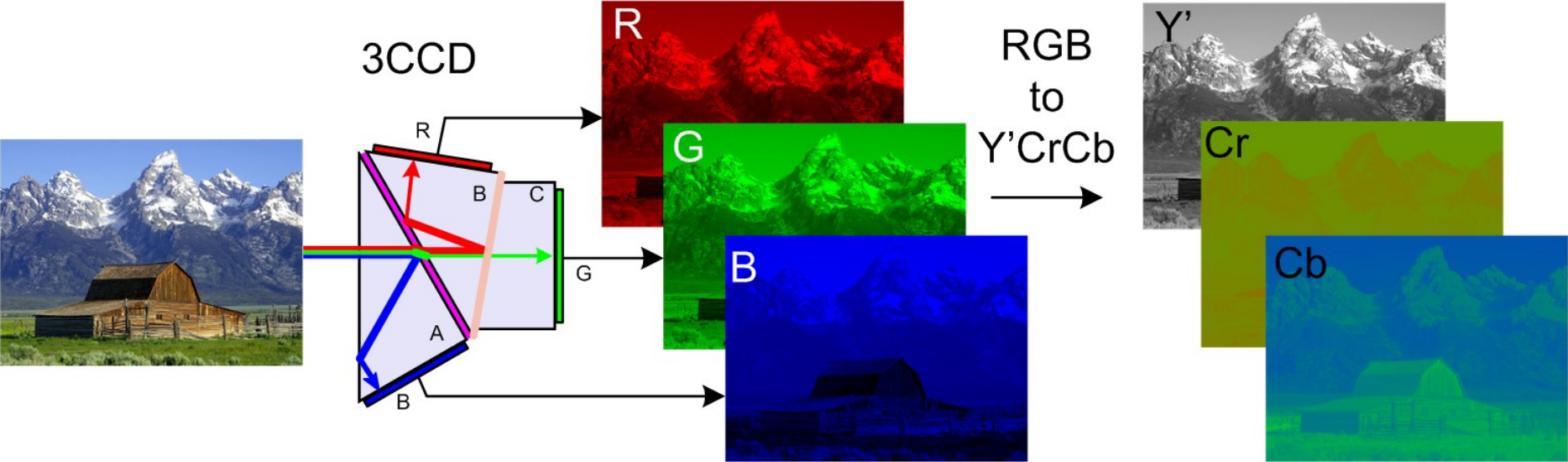
$$Cr = 128 + 0.5R - 0.418688G + 0.081312B$$

$$R = Y + 1.402(Cr - 128)$$

$$G = Y - 0.34414(Cb - 128) - 0.71414(Cr - 128)$$

$$B = Y + 1.772(Cb - 128)$$

YCbCr Color Space



Video camera

Channel Subsampling



Y
x0.5



Cb
x0.5



Cr
x0.5



Channel Subsampling



Y
x1



Cb
x0.5



Cr
x0.5



Channel Subsampling



Y
x1



Cb
x0.1



Cr
x0.1



Channel Subsampling



Y
x1



Cb
x0.05



Cr
x0.05



Channel Subsampling



Y
x1



Cb
x0.01



Cr
x0.01



Channel Subsampling



Y
x0.05



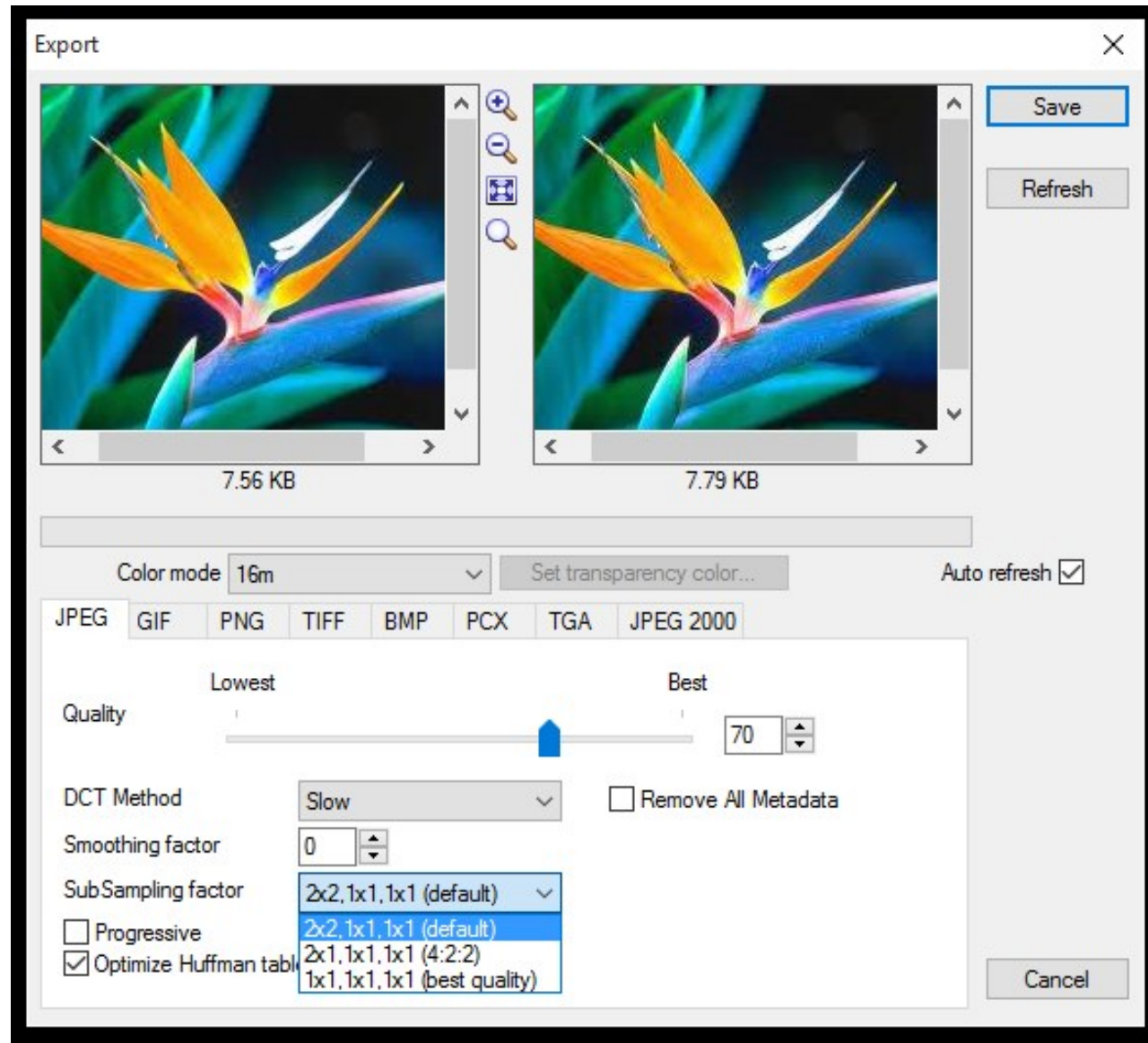
Cb
x1



Cr
x1



Channel Subsampling



Channel Subsampling in JPEG image format

Channel re-quantization



Y
4bit



Cb
4bit



Cr
4bit



Channel re-quantization



Y
8bit



Cb
7bit



Cr
7bit



Channel re-quantization



Y
8bit



Cb
6bit



Cr
6bit



Channel re-quantization



Y
8bit



Cb
5bit



Cr
5bit



Channel re-quantization



Y
8bit



Cb
4bit



Cr
4bit



Channel re-quantization



Y
8bit



Cb
3bit



Cr
3bit



Channel re-quantization



Y
8bit



Cb
2bit



Cr
2bit



Channel re-quantization



Y
4bit



Cb
8bit



Cr
8bit

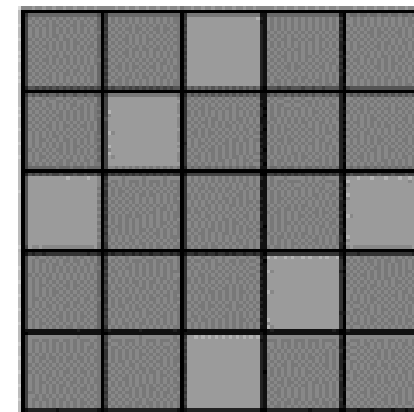
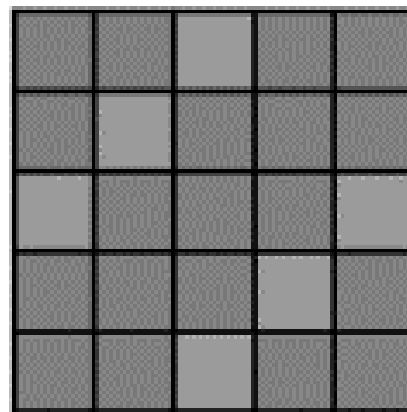
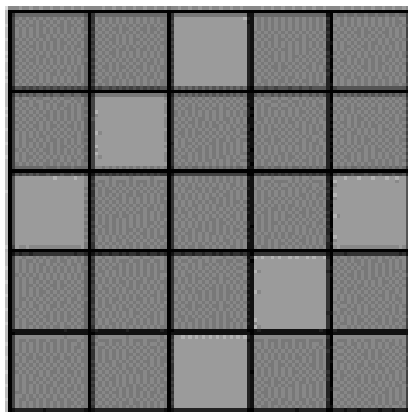
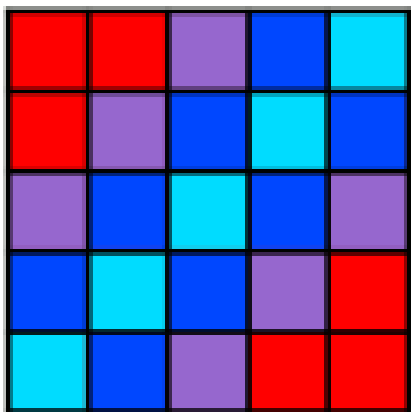


Indexed color

Bitmap

Bitmap

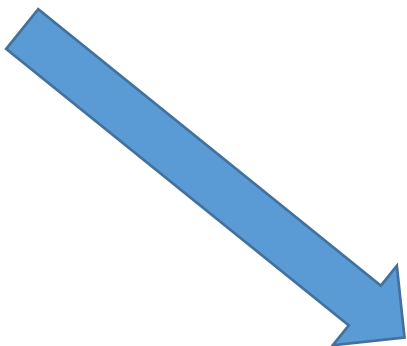
Bitmap



A

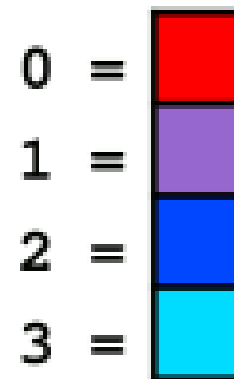
B

C



0	0	1	2	3
0	1	2	3	2
1	2	3	2	1
2	3	2	1	0
3	2	1	0	0

Bitmap



Palettes/ color map

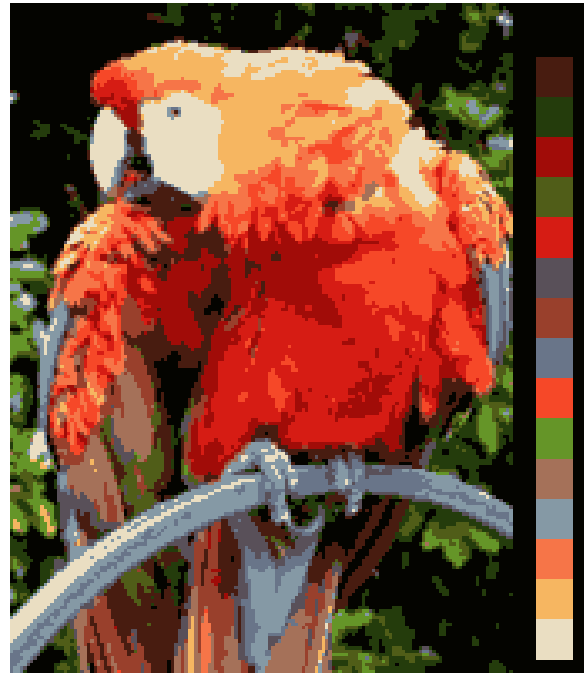
Indexed color



24-Bit



2-Bit



4-Bit



8-Bit

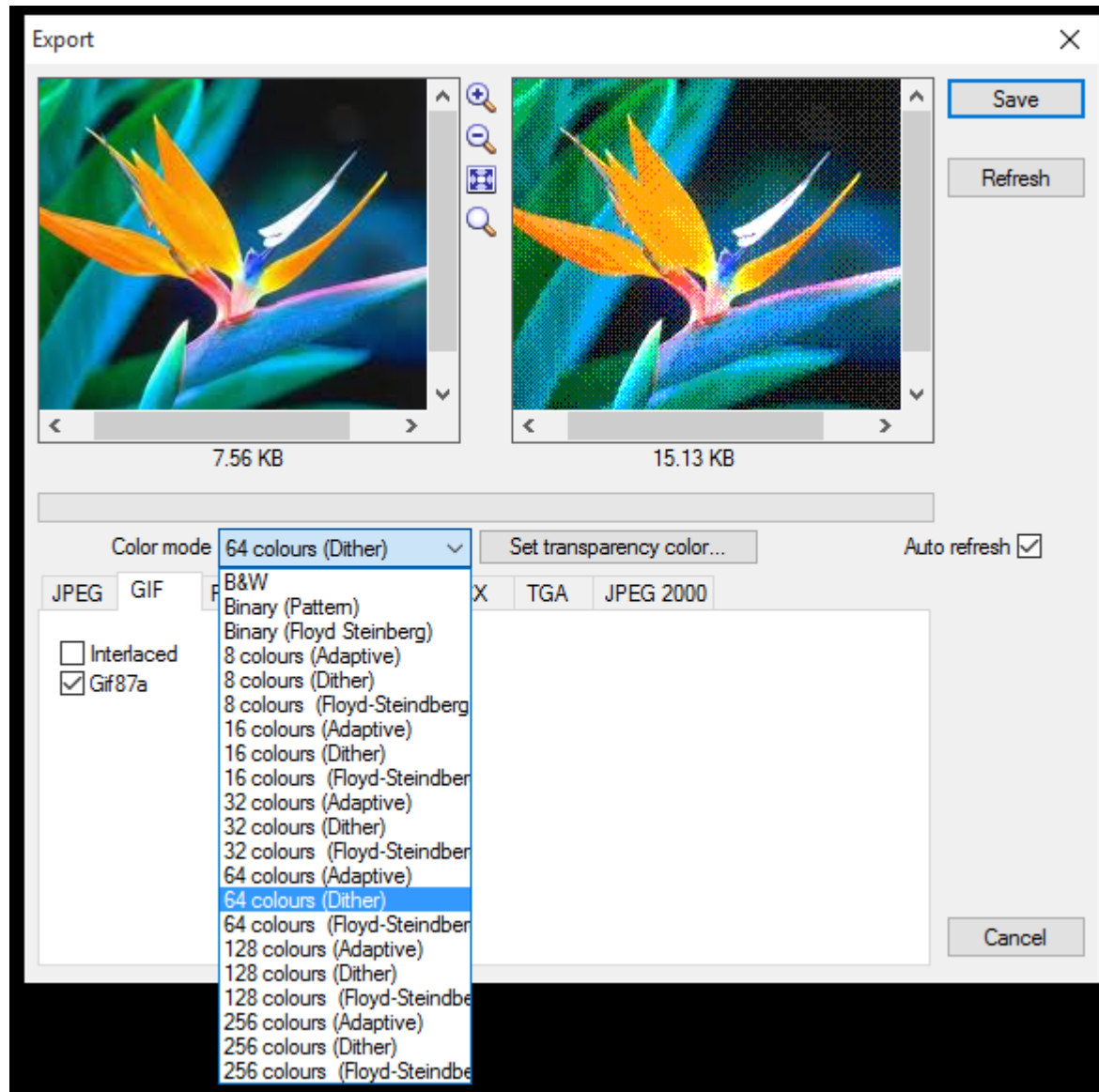
Indexed color

Image file formats supporting indexed color

Acronym	Full name	Creator	DOS extension	1-bit (2)	2-bit (4)	3-bit (8)	4-bit (16)	5-bit (32)	6-bit (64)	7-bit (128)	8-bit (256)	Compression
PCX	PC Paintbrush Image File	ZSoft Corporation	.pcx	Yes	Yes	No	Yes	No	No	No	Yes	RLE
ILBM	InterLeaved BitMap	Electronic Arts	.lbm, .iff	Yes	Yes	Yes	Yes	Yes	Yes* (EHB mode, 64-color)	Yes*	Yes*	Uncompressed, RLE
GIF	Graphics Interchange Format	CompuServe	.gif	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	LZW
TGA	TARGA File format	Truevision	.tga, .vda, .icb, .vst	No	No	No	No	No	No	No	Yes	RLE
TIFF	Tagged Image File Format	Aldus	.tif	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Uncompressed, DEFLATE , LZW , PackBits , CCITT Group 3 fax , CCITT Group 4 fax , JPEG , others less common (**)
BMP	Device-independent Bitmap	Microsoft	.bmp, .dib, .rle	Yes	No	No	Yes	No	No	No	Yes	Uncompressed, RLE (***)
PSD	Photoshop Document	Adobe Systems	.psd	No	No	No	No	No	No	No	Yes	PackBits
PNG	Portable Network Graphics	PNG Development Group	.png	Yes	Yes	No	Yes	No	No	No	Yes	DEFLATE

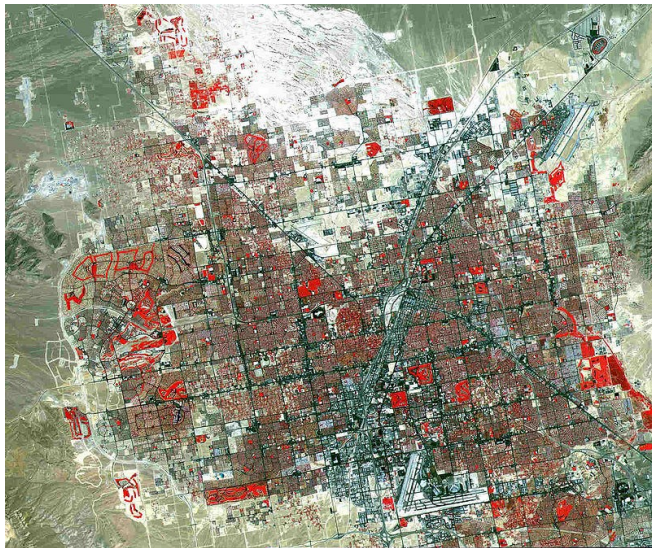
Indexed color

Color mode in GIF image format

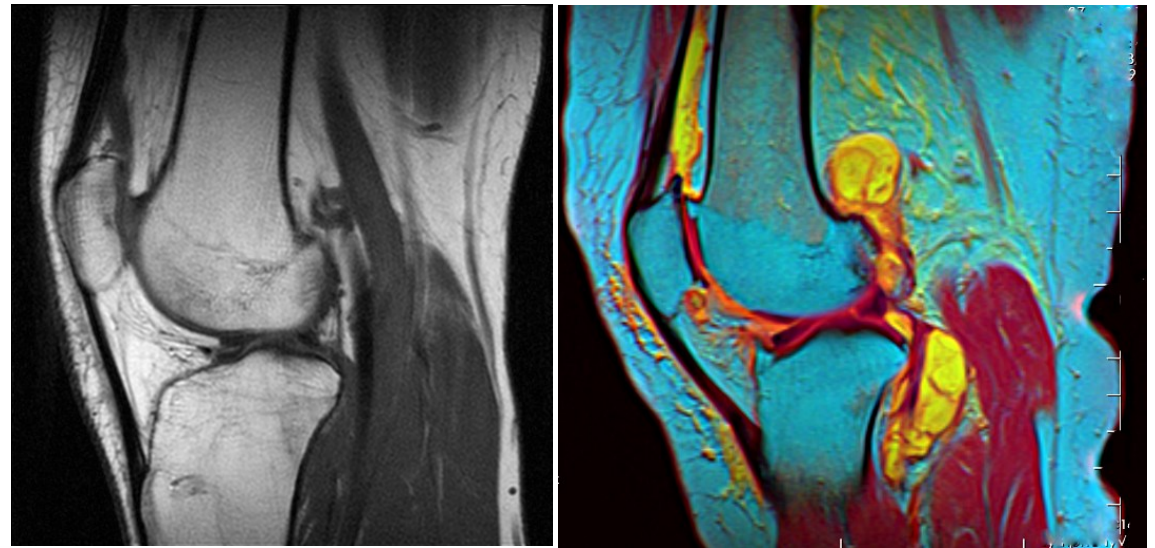


A false-color image sacrifices natural color rendition in order to ease the detection of features that are not readily discernible

A pseudo color image is derived from a grayscale image by mapping each intensity value to a color according to a table or function



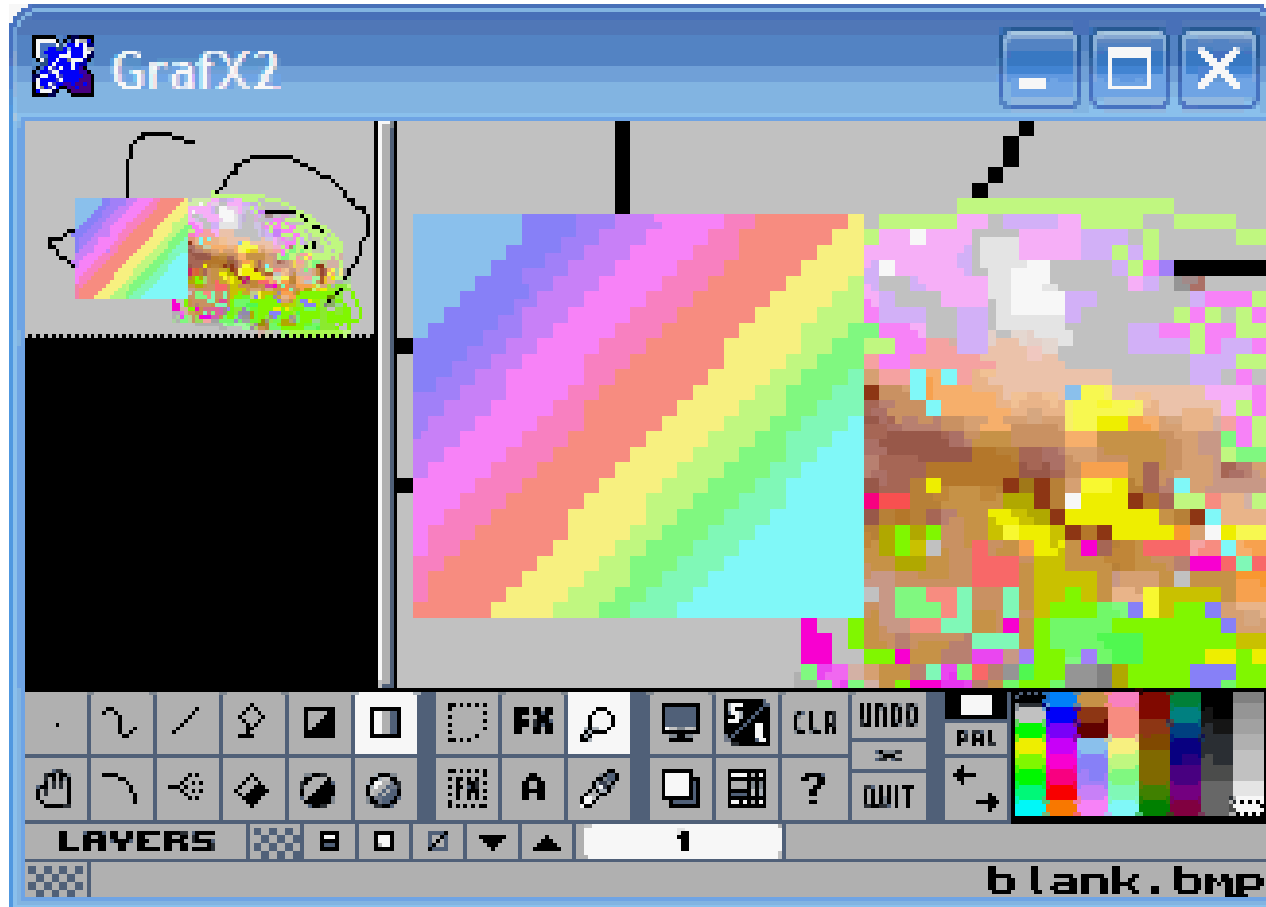
False color



Pseudo color

Indexed color

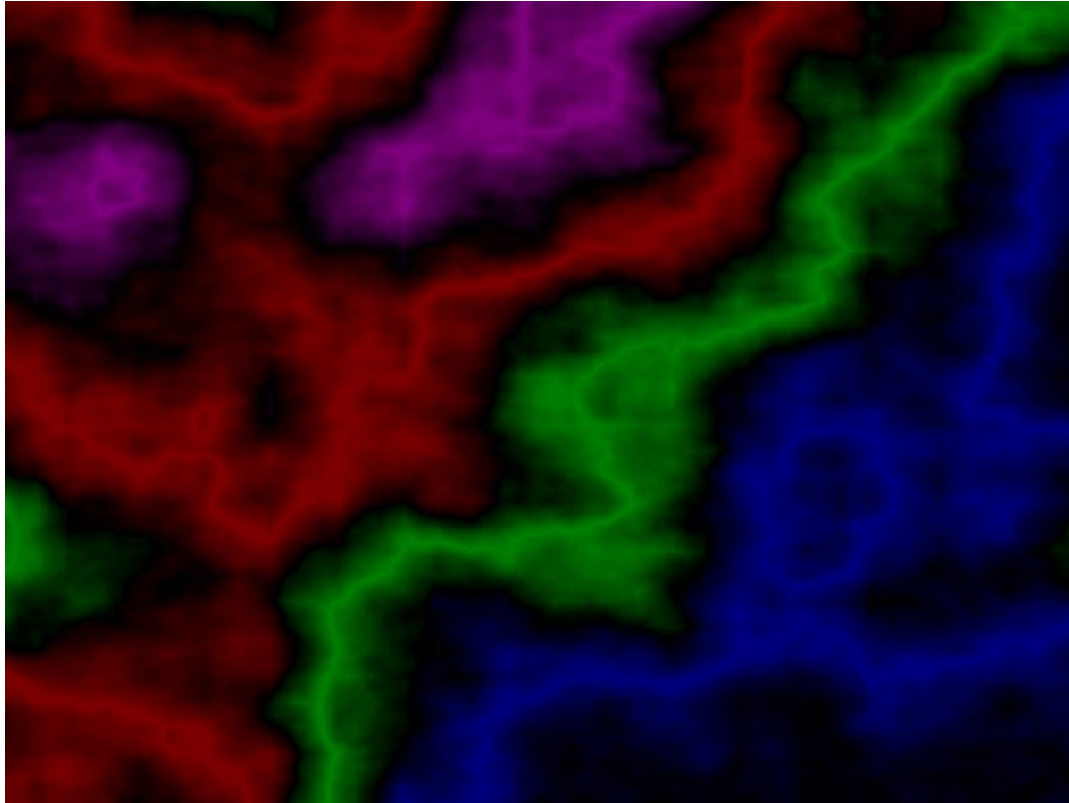
palette shifting



SimCity 2000 made extensive use of this technique: every building with animation had its animation provided by color cycling

Indexed color

palette shifting



<http://www.effectgames.com/demos/canvacycle/?sound=1>



Matlab image processing function

RGB to HSV conversion:

```
lHSV=rgb2hsv(im);
```

HSV to RGB conversion:

```
im=hsv2rgb(lHSV);
```

RGB to YCrCb conversion:

```
im=rgb2ycrcb(rgb);
```

YCrCb to RGB conversion:

```
im=ycrcb2rgb(ycrcb);
```

Change color map:

```
im=ind2rgb(im,colormap('map type'));
```


List of color spaces and their uses

https://en.wikipedia.org/wiki/List_of_color_spaces_and_their_uses

